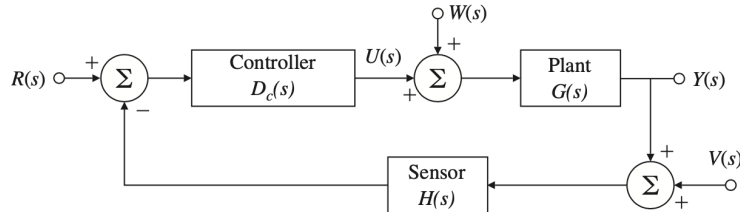


# Final Exam

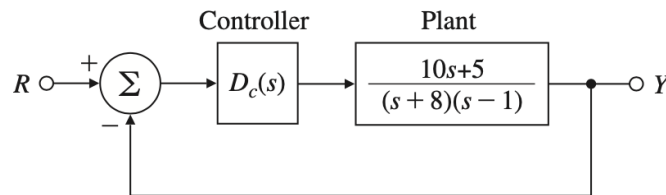
Subject : Control System Engineering 1, Lecturer : Prof. Youngjin Choi,

Date : June 19, 2020 (Contact e-mail : cyj@hanyang.ac.kr)

**Problem 1 (20pt)** Consider the following figure with  $G(s) = \frac{1}{s(\tau s+1)}$ ,  $D_c(s) = k_P + k_D s$  and  $H(s) = 1 + k_t s$ . Determine the system type and relevant error constant with respect to the reference inputs when  $V = W = 0$ .



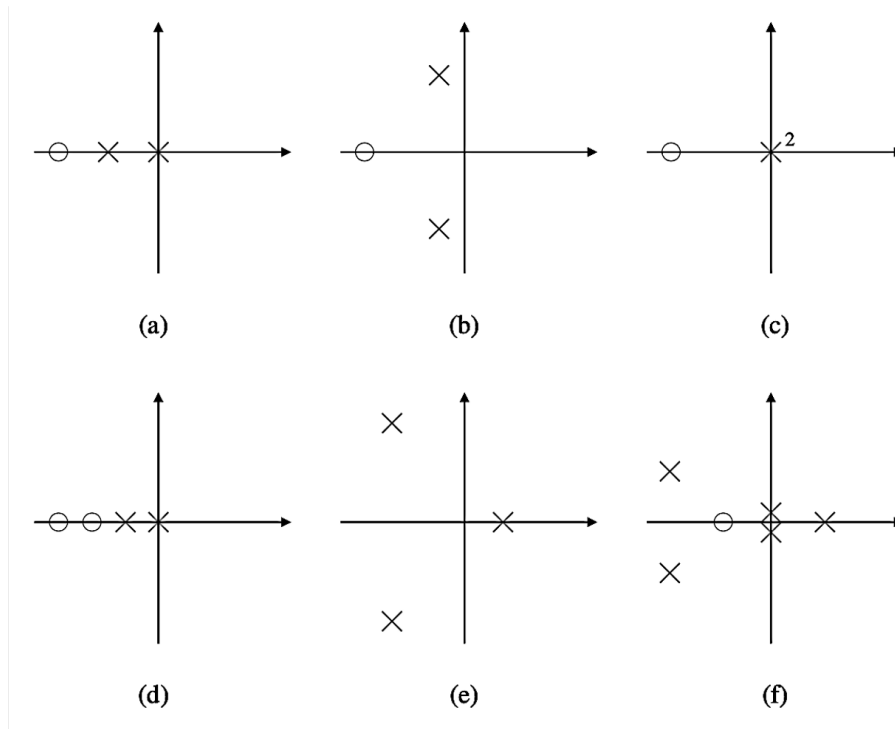
**Problem 2 (20pt)** Consider the controller of the form  $D_c(s) = \frac{1}{s^n}$  with  $n$  being a non-negative integer. For what values of  $n$  is the closed-loop system stable?



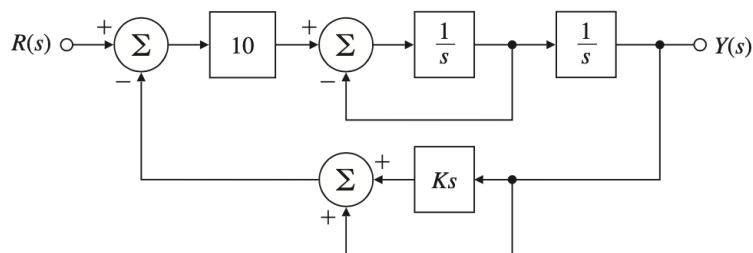
**Problem 3 (20pt)** Roughly sketch the root loci for the following pole-zero maps. Each pole-zero map is from a characteristic equation of the form:

$$1 + K \frac{b(s)}{a(s)} = 0$$

where the roots of the  $b(s)$  are shown as small circles  $\circ$  and the roots of the  $a(s)$  are shown as  $\times$  on the s-plane. Note, in figure (c), there are two poles at the origin.



**Problem 4 (20pt)** For the feedback system shown in the figure, find the value of the gain  $K$  that results in dominant closed-loop poles with a damping ratio  $\zeta = \frac{1}{\sqrt{2}}$



**Problem 5 (20pt)** Draw the root locus with respect to  $K$  for the equation  $1 + KL(s) = 0$ , where the departure angles should be calculated and suggested.

$$L(s) = \frac{s + 3}{s(s + 10)(s^2 + 2s + 2)}$$